

## NOTE

This evidence and algorithm-based strategy is consistent with the recommendations of the National Research Council 2010. The prevention and Treatment of Missing Data in Clinical Trial. Washington, DC: The National Academies Press. https://doi.org/10.17226/12955.

Legend: MAR= Missing at Random; MNAR= Missing not at Random; LOCF = Last Observation Carried Forward; MADRS = Montgomery-Asberg Depression Rating Scale

| Inclusion Criteria   | Exclusion Criteria   |
|--|--|
| • MADRS ≥ 6 and/or clinical diagnosis of MDD based on the Diagnostic and Statistical Manual of Mental Disorders, Fifth Edition (DSM-V) and stable treatment (no dose change for ≥12 weeks) with SSRI;                          | • Active suicidality, psychosis, or dysthymia;   |
| • Confirmed diagnosis of PD based on the Queen Square Brain Bank criteria and mild to moderate PD with a Hoehn and Yahr stage between 1-3 in the "ON" state treated with levodopa at a stable dose (no changes for ≥12 weeks); | • Atypical parkinsonism;   |
| • Age 60 to 90 years old; and  | • Atypical depression;   |
| • Ability to read and understand the written participant study information kit and give informed consent.  | • Cognitive impairment or neurological disease other than PD;  |
|  | <ul> <li>Recent (≤12 weeks) change in levodopa dose;</li> </ul>  |
|  | <ul> <li>Recent (≤12 weeks) change in SSRI dose;</li> </ul>  |
|  | <ul> <li>Recent (≤12 weeks) use of probiotics or antibiotics;</li> <li>Medical conditions such as primary gastrointestinal diseases, acute infectious diseases, immunosuppression, or</li> </ul> |

• History of alcohol or drug abuse.

Table S2. Timeline

| Visit number & time-point         | Remote/on-site | Visit agenda  |
|-----------------------------------|----------------|---|
| Visit 1                           | Remote         | · Study introduction  |
|                                   |                | · Information package about trial provided, participant will be encouraged to ask questions |
|                                   |                | · Appointment time/date and platform for next visit determined                              |
| Visit 2                           | On-site/remote | · Screening - inclusion and exclusion criteria assessed                                     |
|                                   | ,              | · Participants will be encouraged to ask questions  |
|                                   |                | · Informed consent signed   |
|                                   |                | · Participant supplied with treatment for 14-day run-in period                              |
|                                   |                | · Appointment time/date and platform for next visit determined                              |
| Visit 3                           | On-site        | · Adherence to the study protocol during run-in period assessed                             |
| Last day of run-in period         |                | · Baseline assessment using the MADRS and BDI-II  |
|                                   |                | · Adverse events diary provided and explained   |
|                                   |                | · Probiotics/placebo (three months' worth) supplied   |
|                                   |                | · Appointment time/date and platform for next visit   |
|                                   |                | determined  |
| Visit 4                           | On-site        | · 1-month safety assessment   |
| Day 30 $\pm$ 3-day, 6-day window  |                | · Changes in levodopa dose assessed   |
|                                   |                | · Adverse events assessed   |
|                                   |                | · Returned pills counted and adherence assessed   |
|                                   |                | · Appointment time/date and platform for next visit   |
|                                   |                | determined  |
| Visit 5                           | On-site        | · 3-month assessment using the MADRS and BDI-II   |
| Day 90 $\pm$ 7-day, 14-day window | Į.             | · Changes in levodopa dose assessed   |
|                                   |                | · Adverse events assessed   |
|                                   |                | · Returned pills counted and adherence assessed   |
|                                   |                | · Probiotics/placebo (three months' worth) supplied   |
|                                   |                | · Appointment time/date and platform for next visit determined                              |